

# **Bounds analysis of unemployment durations in Germany**

**Sokbae (Simon) Lee**

**IFS and UCL**

**and**

**Ralf Wilke**

**ZEW Mannheim**

## Introduction

- This project is concerned with estimating effects of the reform of the German unemployment compensation system during the 1980s.
- Natural experiment: for elderly unemployed workers, the maximum entitlement periods for unemployment benefits have increased during the mid 1980s. See Hunt (1995) and Fitzenberger and Wilke (2004).

- Early retirement issue for aged  $>50$ : Sample composition depends on treatment. Restrict analysis to aged  $<50$ .
- Hunt (1995) found evidence for significant effects of extension of unemployment benefits using German Socioeconomic Panel (survey data). Fitzenberger/Wilke (2004) found that results depend on the definition of unemployment using IAB employment subsample (IABS, register data).

- The goal of this project is to revisit Hunt's findings using IABS 1975-1997.
- In particular we aim to provide robust results in terms of definition of unemployment and to overcome possible selection problems.

## Data

- IAB employment subsample is register based data of individuals of about 500,000 individuals in West-Germany.
- This has much larger sample size compared to German Socioeconomic Panel, but unemployment spells are not identified from the data.
- The data contains daily information on employment spells and the spells during which individuals receive transfer payments from the labor offices.
- We expect less measurement error regarding the unemployment spells than in survey data.

## Data (continued)

- Proxies for unemployment (Fitzenberger/Wilke, 2004)
  - Nonemployment (NE): All periods of nonemployment during which the individual receives at least for one day income transfer payments.
  - Unemployment between jobs (UBJ): Periods between employment spells during which an individual continuously receives income transfer payments.
- NE is an upper bound of the unobserved unemployment spell and UBJ is a lower bound.

## Data (continued)

- Reform years: 1985-1987
- Pre-reform years: 1981 - 1983 (3 years)
  - Unemployment spells starting in 1983 are the latest not affected by the reform.
- Post-reform years: 1987 - 1994 (8 years)
  - The post reform system applies to most of the unemployment spells starting in 1987.
- Control group: workers aged 26-41
  - Aged  $<25$  excluded because of youth unemployment policy changes.

## Data (continued)

- Treatment group: workers aged 44-48
  - Aged 42-43 are excluded because the treatment for this group is weak.
  - Aged  $>48$  are not considered because of early retirement issue.
- Sample restricted to:
  - only periods with unemployment benefits as first income transfer
  - only individuals not receiving any unemployment transfer during the past 12 months and who did not get a recall to the former employer after the last unemployment period.
  - only individuals with completed apprenticeship or university degree
  - business sector agriculture is excluded



## Data (continued)

Table 1: Descriptive summary of the sample: pre reform years

	aged 26-41	aged 44-48
	(control group)	(treatment group)
number of spells	8,194	1,481
mean/median spell length UBJ	101/18	114/44
mean/median spell length NE	664/267	494/197
censored (NE)	12%	16%
female	44%	32%
married	75%	81%
mean age (in years)	32.1	45.8

## Data (continued)

Table 2: Descriptive summary of the sample: post reform years

	aged 26-41	aged 44-48
	(control group)	(treatment group)
number of spells	20,135	3,271
mean/median spell length UBJ	99/10	114/6
mean/median spell length NE	463/260	521/307
censored (NE)	21%	28%
female	50%	44%
married	55%	69%
mean age (in years)	32.2	45.9

## Econometric Framework

- Our framework is based on bounds analysis (Manski 2003).
- In particular, we present bounds for treatment effects in the context of difference-in-differences.
- Tighter bounds are obtained using some monotonicity and independence assumptions. See Manski and Pepper (2000) and Blundell, Gosling, Ichimura, and Meghir (2004) among others.
- No new ideas; however, our project appears to be a first application of bounds analysis to duration analysis and difference-in-differences.

## Interval data on durations

- Assume that we observe interval data on durations, that is we observe  $Y_1$  and  $Y_2$ , where  $Y_1 \leq Y_2$ . It is only known that latent duration  $Y$  is between  $Y_1$  and  $Y_2$ . For example, if  $Y_1 = Y_2$ , then observed duration is a point; however, in general, we have  $Y_1 < Y_2$ , including standard right-censored cases.
- Define  $S(y|x) = P(Y > y|X = x)$ ,  $S_1(y|x) = P(Y_1 > y|X = x)$ , and  $S_2(y|x) = P(Y_2 > y|X = x)$ . With the empirical evidence alone, then the identification region for  $S(y|x)$  is

$$(1) \quad S_1(y|x) \leq S(y|x) \leq S_2(y|x).$$

## Bounding the treatment effect

- In addition to covariates  $X$ , suppose that  $P$  denotes time periods 0 and 1 (before and after a reform) and  $T$  denotes age groups 0 and 1 (control and treatment groups).
- Consider the treatment effect on the survival probability  $S(y|x)$ . The effect of a reform can be measured by difference-in-differences.
- Note that the effect of a reform can be estimated by a sample analog of

$$\begin{aligned}\Delta(y|x) = & [S(y|T = 1, P = 1, X = x) - S(y|T = 0, P = 1, X = x)] \\ & - [S(y|T = 1, P = 0, X = x) - S(y|T = 0, P = 0, X = x)]\end{aligned}$$

## Bounding the treatment effect (continued)

- Using the empirical evidence alone,

$$(2) \quad S_1(y|t, p, x) \leq S(y|t, p, x) \leq S_2(y|t, p, x)$$

for  $t = 0, 1$  and  $p = 0, 1$ .

- Hence,

$$\begin{aligned} S_1(y|1, 1, x) - S_2(y|0, 1, x) &\leq S(y|1, 1, x) - S(y|0, 1, x) \\ &\leq S_2(y|1, 1, x) - S_1(y|0, 1, x) \end{aligned}$$

and

$$\begin{aligned} S_1(y|1, 0, x) - S_2(y|0, 0, x) &\leq S(y|1, 0, x) - S(y|0, 0, x) \\ &\leq S_2(y|1, 0, x) - S_1(y|0, 0, x). \end{aligned}$$

## Bounding the treatment effect (continued)

- This implies that  $\Delta(y|x)$  is bounded by an interval with endpoints  $[l(y|x), u(y|x)]$

$$l(y|x) = \max[-1, \{S_1(y|1, 1, x) - S_2(y|0, 1, x)\} \\ - \{S_2(y|1, 0, x) - S_1(y|0, 0, x)\}]$$

and

$$u(y|x) = \min[1, \{S_2(y|1, 1, x) - S_1(y|0, 1, x)\} \\ - \{S_1(y|1, 0, x) - S_2(y|0, 0, x)\}].$$

- If this interval is shorter than  $[-1, 1]$ , there is identifying power. In particular, the lower bound is larger than zero or the upper bound is smaller than zero, then that will provide the sign of the effect.

## Imposing additional assumptions

- **[Assumption S1]** Suppose that  $S(y|0, p, x) \leq S(y|1, p, x)$  for all  $p$  and  $x$ .
- This means that young workers tend to have shorter durations than old workers while other things being equal.
- Under this additional assumption,

$$\begin{aligned} \max\{0, S_1(y|1, 1, x) - S_2(y|0, 1, x)\} &\leq S(y|1, 1, x) - S(y|0, 1, x) \\ &\leq S_2(y|1, 1, x) - S_1(y|0, 1, x) \end{aligned}$$

and

$$\begin{aligned} \max\{0, S_1(y|1, 0, x) - S_2(y|0, 0, x)\} &\leq S(y|1, 0, x) - S(y|0, 0, x) \\ &\leq S_2(y|1, 0, x) - S_1(y|0, 0, x). \end{aligned}$$



## Imposing additional assumptions (continued)

- This implies that  $\Delta(y|x)$  is bounded by an interval with endpoints  $[\tilde{l}(y|x), \tilde{u}(y|x)]$

$$\begin{aligned}\tilde{l}(y|x) = & \max[-1, \max\{0, S_1(y|1, 1, x) - S_2(y|0, 1, x)\} \\ & - \{S_2(y|1, 0, x) - S_1(y|0, 0, x)\}]\end{aligned}$$

and

$$\begin{aligned}\tilde{u}(y|x) = & \min[1, \{S_2(y|1, 1, x) - S_1(y|0, 1, x)\} \\ & - \max\{0, S_1(y|1, 0, x) - S_2(y|0, 0, x)\}].\end{aligned}$$

## Imposing additional assumptions (continued)

- **[Assumption S2]** Suppose that  $S(y|t, p, x, v) \leq S(y|t, p, x, v')$  for  $v \leq v'$ .
- In other words, the survivor function is monotone with respect to  $v$ . For example, let  $V$  be the age of a worker in years. Then this says that the survivor function is increasing as a worker gets older conditional on other variables.
- Then

$$(3) \quad \max_{v' \leq v} S_1(y|t, p, x, v') \leq S(y|t, p, x, v) \leq \min_{v' \geq v} S_2(y|t, p, x, v')$$

for  $t = 0, 1$  and  $p = 0, 1$ .

## Imposing additional assumptions (continued)

- By the law of iterative expectations,

$$(4) \quad T_1(y|t, p, x) \leq S(y|t, p, x) \leq T_2(y|t, p, x),$$

where

$$T_1(y|t, p, x) = \sum_v \Pr(V = v|t, p, x) [\max_{v' \leq v} S_1(y|t, p, x, v')]$$

and

$$T_2(y|t, p, x) = \sum_v \Pr(V = v|t, p, x) [\min_{v' \geq v} S_2(y|t, p, x, v')].$$

## Imposing additional assumptions (continued)

- Combining this with Assumption S1 gives a tighter bound for  $\Delta(y|x)$ :

$$\bar{l}(y|x) = \max[\tilde{l}(y|x), \max\{0, T_1(y|1, 1, x) - T_2(y|0, 1, x)\} \\ - \{T_2(y|1, 0, x) - T_1(y|0, 0, x)\}]$$

and

$$\bar{u}(y|x) = \min[\tilde{u}(y|x), \{T_2(y|1, 1, x) - T_1(y|0, 1, x)\} \\ - \max\{0, T_1(y|1, 0, x) - T_2(y|0, 0, x)\}].$$

## Imposing additional assumptions (continued)

- To further shorten the interval, one may assume that  $\Delta(y|x) = \Delta(y)$  for all  $x$  in some set  $\mathcal{X}$ . That is, the treatment effect is independent of  $x \in \mathcal{X}$ .
- Then

$$\Delta(y) \in [\max_{x \in \mathcal{X}} l(y|x), \min_{x \in \mathcal{X}} u(y|x)]$$

for some upper and lower bounds  $l(y|x)$  and  $u(y|x)$ .

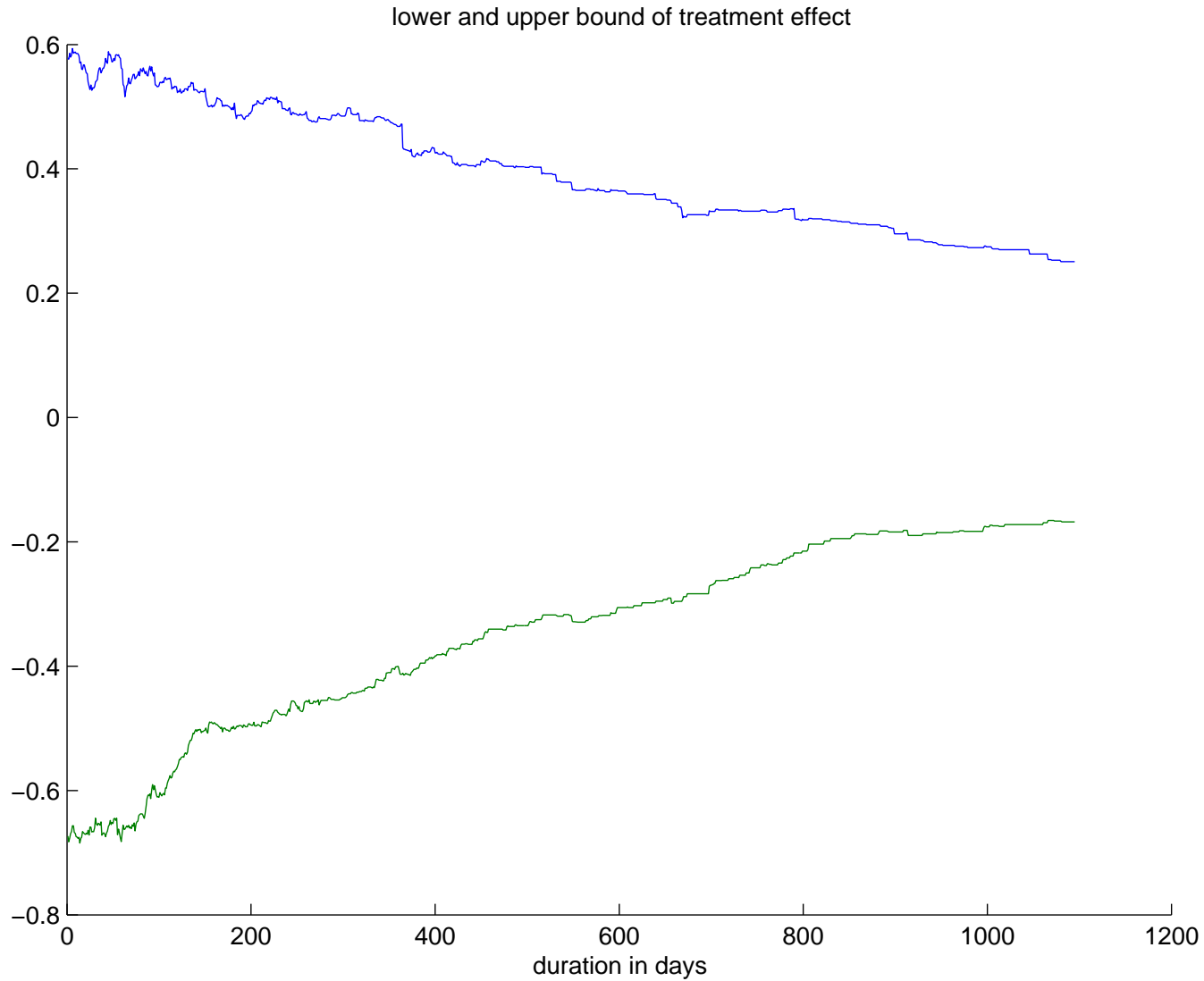


Figure 1. Without S1 and S2 (Male; Married)

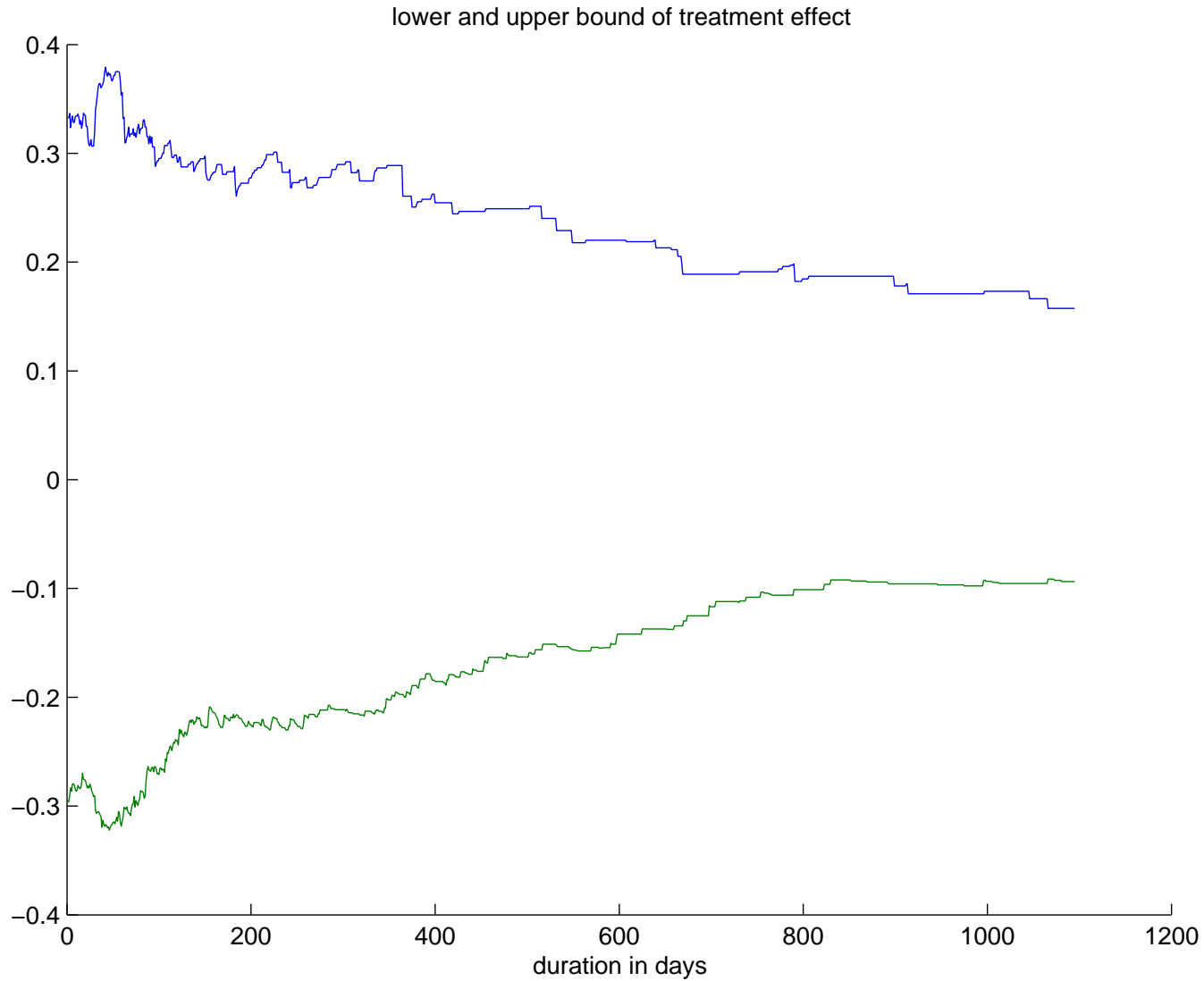


Figure 2. With only S1 (Male; Married)

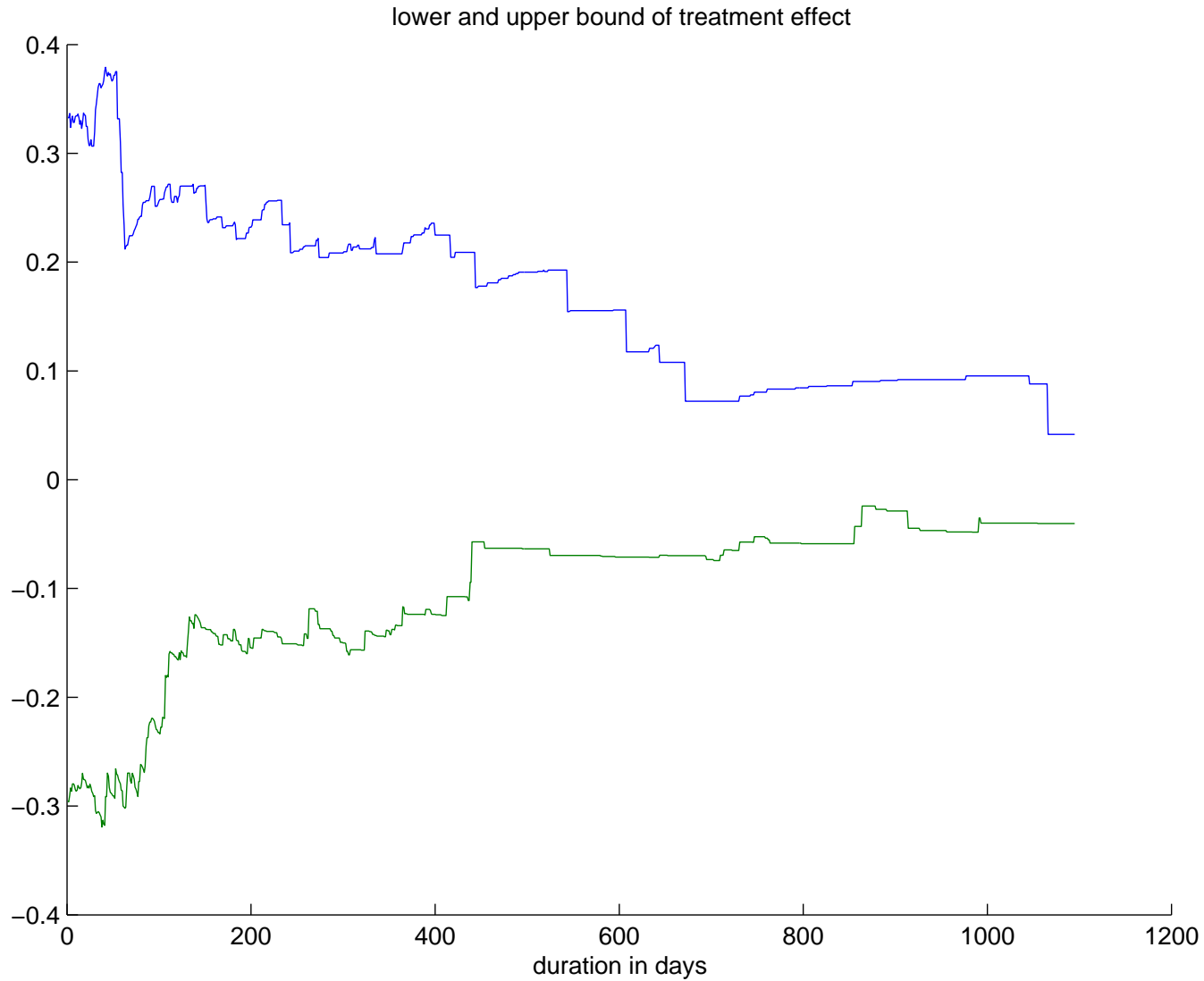


Figure 3. With S1 and S2 (Male; Married)



## Bounding quantile treatment effects

- Notice (1) can be rewritten in terms of conditional quantile functions:

$$(5) \quad Q_1(\tau|x) \leq Q(\tau|x) \leq Q_2(\tau|x),$$

where  $Q(\tau|x)$  is the  $\tau$ -th quantile of  $Y$  conditional on  $X = x$  and  $Q_j(\tau|x)$  is the  $\tau$ -th quantile of  $Y_j$  conditional on  $X = x$  for  $j = 1, 2$ .

- Invoking difference-in-differences strategy to identify quantile treatment effects (see, for example, Athey and Imbens, 2002), we have

$$\begin{aligned} \Delta_Q(\tau|x) = & [Q(\tau|T = 1, P = 1, X = x) - Q(\tau|T = 1, P = 0, X = x)] \\ & - [Q(\tau|T = 0, P = 1, X = x) - Q(\tau|T = 0, P = 0, X = x)]. \end{aligned}$$

## Bounding quantile treatment effects (continued)

- Hence, using the empirical evidence alone, we have a bound for  $\Delta_Q(\tau|x)$ :

$$l_Q(\tau|x) = [Q_1(\tau|1, 1, x) - Q_2(\tau|1, 0, x)] - [Q_2(\tau|0, 1, x) - Q_1(\tau|0, 0, x)]$$

and

$$u_Q(\tau|x) = [Q_2(\tau|1, 1, x) - Q_1(\tau|1, 0, x)] - [Q_1(\tau|0, 1, x) - Q_2(\tau|0, 0, x)].$$

## Bounding quantile treatment effects (continued)

- As before, we can make additional assumptions.
- **Assumption Q1:**  $Q(\tau|0, p, x) \leq Q(\tau|1, p, x)$
- Note that Assumption Q1 is equivalent to Assumption S1 if Assumption Q1 holds for each  $\tau$ .
- Under this, we have a tighter bound

$$\tilde{l}_Q(\tau|x) = \max[0, Q_1(\tau|1, 1, x) - Q_2(\tau|0, 1, x)] - [Q_2(\tau|1, 0, x) - Q_1(\tau|0, 0, x)]$$

and

$$\tilde{u}_Q(\tau|x) = [Q_2(\tau|1, 1, x) - Q_1(\tau|0, 1, x)] - \max[0, Q_1(\tau|1, 0, x) - Q_2(\tau|0, 0, x)].$$

## Bounding quantile treatment effects (continued)

• **Assumption Q2:**  $Q(\tau|t, p, x, v) \leq Q(\tau|t, p, x, v')$  for  $v \leq v'$  for any  $\tau$ .

• Equivalently,  $F(y|t, p, x, v) \geq F(y|t, p, x, v')$  for  $v \leq v'$ , where  $F$  denotes a conditional CDF. Then

$$(6) \quad \max_{v' \geq v} F_2(y|t, p, x, v') \leq F(y|t, p, x, v) \leq \min_{v' \leq v} F_1(y|t, p, x, v')$$

for  $t = 0, 1$  and  $p = 0, 1$ .

## Bounding quantile treatment effects (continued)

- By the law of iterative expectations,

$$(7) \quad R_2(y|t, p, x) \leq F(y|t, p, x) \leq R_1(y|t, p, x),$$

where

$$R_2(y|t, p, x) = \sum_v \Pr(V = v|t, p, x) \left[ \max_{v' \geq v} F_2(y|t, p, x, v') \right]$$

and

$$R_1(y|t, p, x) = \sum_v \Pr(V = v|t, p, x) \left[ \min_{v' \leq v} F_1(y|t, p, x, v') \right].$$

## Bounding quantile treatment effects (continued)

- Notice that for any two invertible functions  $f(x)$  and  $g(x)$ ,  $f(x) \leq g(x)$  if and only if  $f^{-1}(x) \geq g^{-1}(x)$ . Using this,

$$R_1^{-1}(\tau|t, p, x) \leq Q(\tau|t, p, x) \leq R_2^{-1}(\tau|t, p, x),$$

where  $R_j^{-1}(\cdot|t, p, x)$  is the inverse of  $R_j(\cdot|t, p, x)$  given  $(t, p, x)$  for  $j = 1, 2$ .

## Bounding quantile treatment effects (continued)

- Combining this with Assumption Q1 gives a tighter bound for  $\Delta_Q(\tau|x)$ :

$$\bar{l}_Q(\tau|x) = \max[\tilde{l}_Q(\tau|x),$$

$$\max[0, R_1^{-1}(\tau|1, 1, x) - R_2^{-1}(\tau|0, 1, x)] - [R_2^{-1}(\tau|1, 0, x) - R_1^{-1}(\tau|0, 0, x)]$$

and

$$\bar{u}_Q(\tau|x) = \min[\tilde{u}_Q(\tau|x),$$

$$[R_2^{-1}(\tau|1, 1, x) - R_1^{-1}(\tau|0, 1, x)] - \max[0, R_1^{-1}(\tau|1, 0, x) - R_2^{-1}(\tau|0, 0, x)]$$

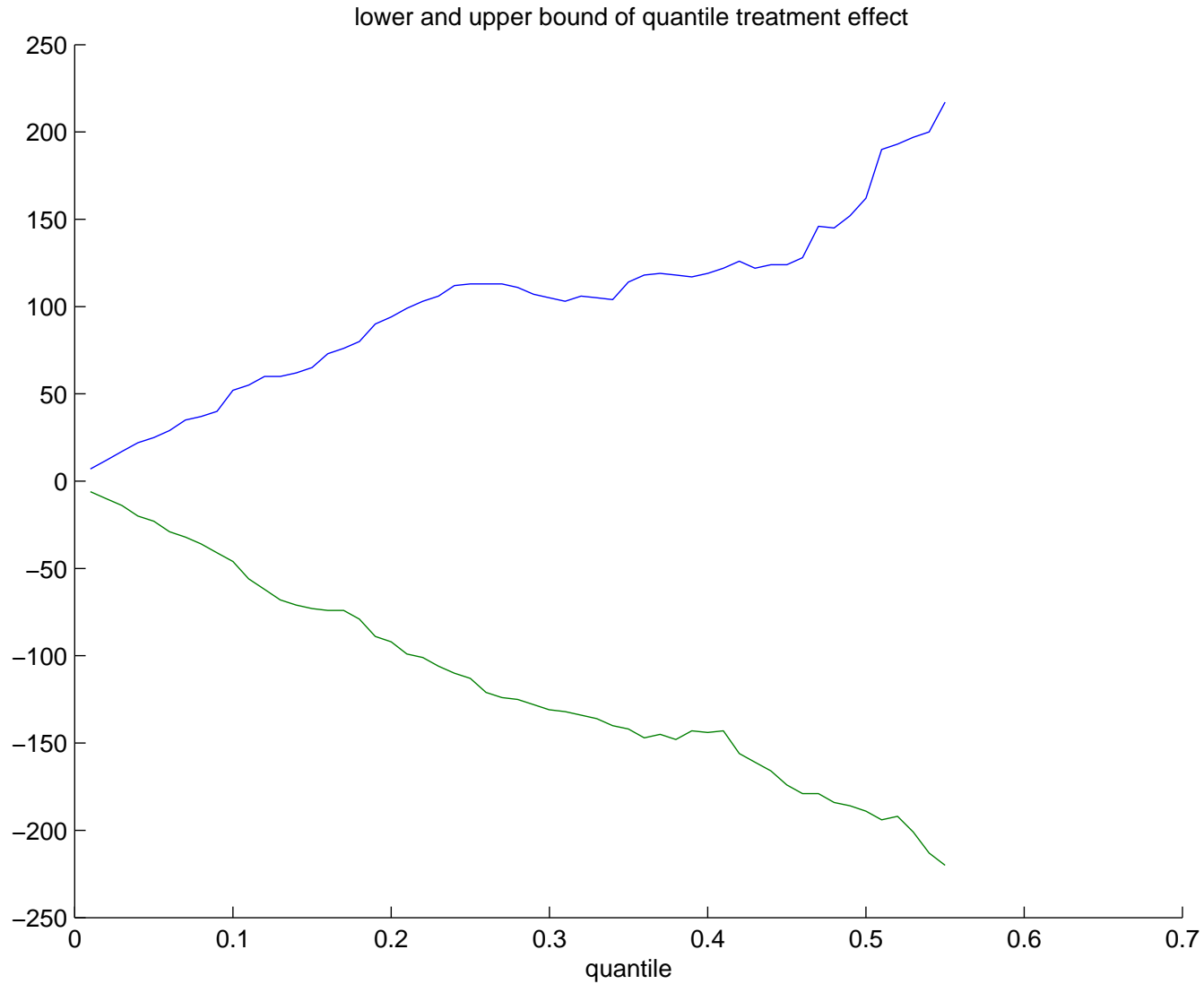


Figure 4. Without Q1 and Q2 (Male; Married)



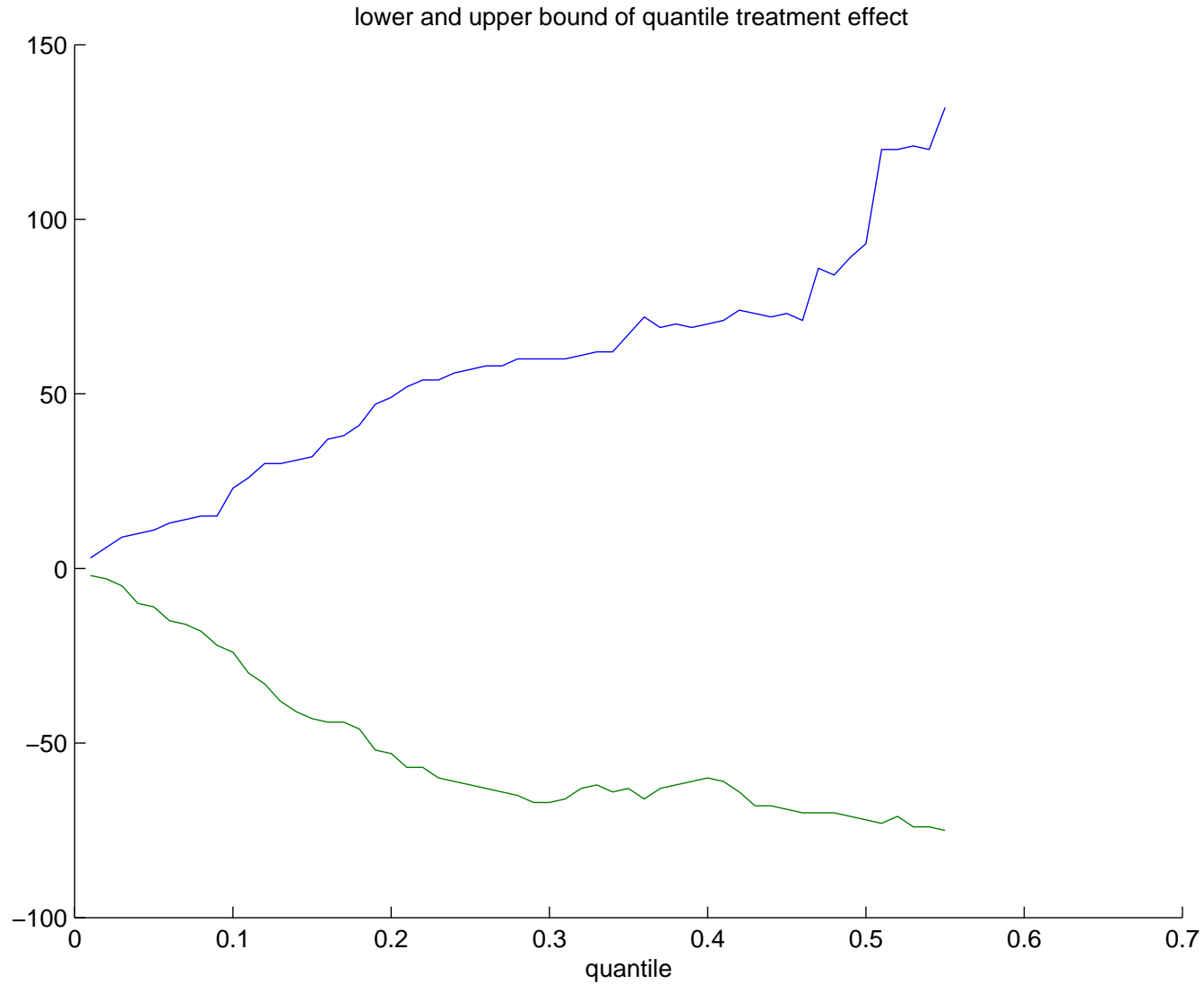


Figure 5. With only Q1 (Male; Married)

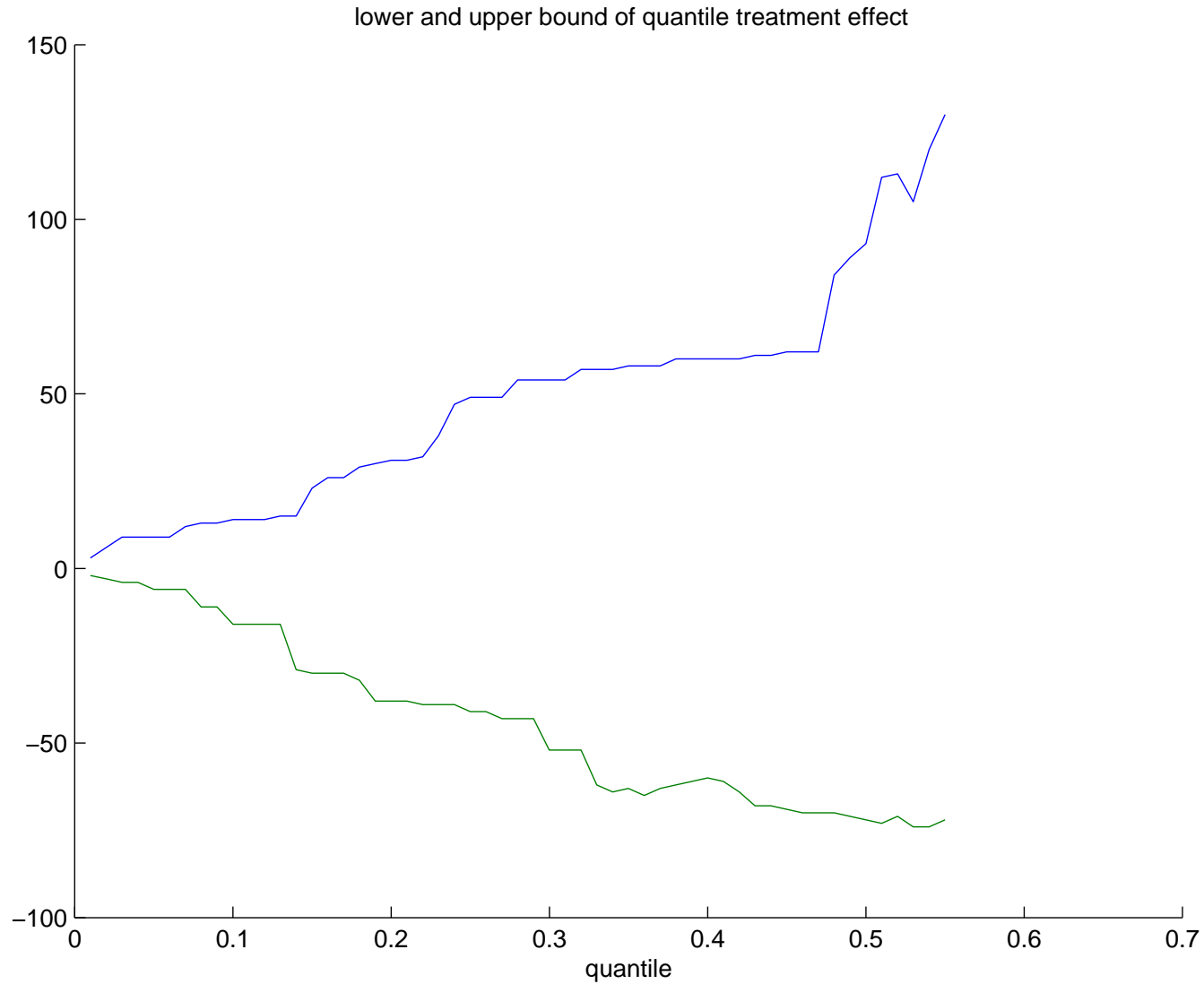


Figure 6. With Q1 and Q2 (Male; Married)

## Conclusion and Future Work

- No evidence for supporting the claim that extensions of unemployment benefits increased unemployment durations.
- One may use a parametric duration model to further tighten the bounds.