

# D1.1: Interim Report: Baseline model for FRAME. A Framework to Study the Macroeconomic Effects of Innovation Policy. Revised.

**Deliverable D1.1:** Interim Report: Baseline model for FRAME. A Framework to Study the Macroeconomic Effects of Innovation Policy. **Revised.** 

Author: Diego Comin and Mario Giarda

Version: 2.0

Quality review: All Partners

**Date:** July 31st, 2018

Grant Agreement number: 727073

**Starting Date:** 01/04/2017



**Duration:** 24 months

Coordinator: Dr. Georg Licht, ZEW

Email: licht@zew.de



# Contents

1	Introduction			
2	Model			
	2.1	Production Sector and Endogenous TFP: Preliminaries	6	
	2.2	R&D and Adoption	7	
		2.2.1 R&D: Creation of $Z_t$		
		2.2.2 Adoption: From $Z_t$ to $A_t$	9	
	2.3	Households	11	
	2.4	Firms	12	
		2.4.1 Intermediate goods firms: factor demands	12	
		2.4.2 Final goods producers: price setting	13	
		2.4.3 Capital producers: investment	14	
		2.4.4 Employment agencies and wage adjustment	14	
		2.4.5 Fiscal and monetary policy	15	
	2.5	Resource constraints and equilibrium	16	
	2.6	Calibration	17	
3	The	e effect of Aggregate Shocks	20	
4	The	effect of government investment in R&D	21	
	4.1	Lump-sum taxes	21	
	4.2	The effect on returns and the skill premium		
	4.3	Distortionary taxation and the role of wage rigidities		
5	Con	nclusion	27	
A	Log-linearization of returns 3			
	. Log inicalization of fourth			



# **Project Information Summary**

Table 1: Project Information Summary

Project Acronym	FRAME
Project Full Title	Framework for the Analysis of Research and Adoption
	Activities and their Macroeconomic Effects
Grant Agreement	727073
Call Identifier	H2020-SC6-CO-CREATION-2016 -1
Topic	CO-CREATION-08-2016/2017: Better integration of evidence
	on the impact of research and innovation in policy making
Funding Scheme	Medium-scaled focused research project
Project Duration	1st April 2017 – 31st March 2019 (24 months)
Project Officer(s)	Hinano SPREAFICO (Research Executive Agency)
	Roberto MARTINO (DG Research and Innovation)
Co-ordinator	Dr. Georg Licht, Zentrum für Europäische Wirtschaftsforschung GmbH
Consortium Partners	Centre for Economic Policy Research
	Lunds Universitet
	Università Luigi Bocconi
	Universitat Pompeu Fabra
	London Business School
Website	http://www.h2020frame.eu/frame/home.html

# **Deliverable Documentation Sheet**



Table 2: Deliverable Documentation Sheet

Number	D1.1
Title	Interim Report: Baseline model for FRAME. A Framework to Study
	the Macroeconomic Effects of Innovation Policy. Revised.
Related WP	WP1
Lead Beneficiary	UPF
Author(s)	Diego Comin (CEPR), Mario Giarda (UPF)
Contributor(s)	
Reviewer(s)	All partners
Nature	R (Report)
Dissemination level	PU (Public)
Due Date	31.07.2018
Submission Date	
Status	

# Quality Control Assessment Sheet

Table 3: Quality Control Assessment Sheet

Issue	Date	Comment	Author
V0.1	30.09.2017	First draft	Diego Comin, Mario Giarda
V1.1	31.03.2018	Second deliverable	Diego Comin, Mario Giarda
V1.2	24.07.2018	Second deliverable revised	Diego Comin, Mario Giarda



## Executive summary

In this first work package, we develop the baseline model that we will use in various of the work packages of FRAME. This model will be used to analyze the impact of various public innovation policies on the evolution of the economy. Our starting point is Anzoategui et al. (2015) who adopt the medium-term cycles framework developed by Comin and Gertler (2006) and introduce price and wage rigidities as well as a monetary policy rule. Effectively, this is a Neo-Keynesian business cycles framework augmented to have endogenous development and diffusion of new technologies.

A key aspect of the work package consists in modelling a wide array of innovation policies with the aim of exploring their impact on the economy dynamics. To this end, we differentiate between three types of innovation policies. First, standard R&D subsidies. Second, hiring scientists to conduct public R&D. Public R&D is socially desirable because it increases the productivity of private R&D. Third, hiring scientists to facilitate the adoption of new technologies by private companies. We impose a government budget constraint and consider two types of taxes, lump sum and distortionary labor income taxes.

We find that public innovation in the form of any of our policies (direct investment or innovation subsidies) expand the economy in the medium term. This implies that it can serve as a substitute for private investment in innovation. We also show that their effects on the economy depend crucially on some parameters, in particular those related with labor markets. We showed that a great degree of wage rigidities hide the aggregate trade-offs generated by labor tax raises. However, even with these trade-offs acting, innovation policies have a positive impact in the aggregate economy, wealth, consumption, and GDP.



## 1 Introduction

In this first work package, we develop the baseline model that we will use in various of the work packages of FRAME. This model will be used to analyze the impact of various public innovation policies on the evolution of the economy. Our starting point is Anzoategui et al. (2015) who adopt the medium-term cycles framework developed by Comin and Gertler (2006) and introduce price and wage rigidities as well as a monetary policy rule. Effectively, this is a Neo-Keynesian business cycles framework augmented to have endogenous development and diffusion of new technologies.

Comin and Gertler (2006) differentiate between the stock of developed technologies and the stock of used technologies. This distinction introduces an adoption lag that is endogenous and time-varying. In particular, the response of private investments in adopting new technologies to business cycle conditions may affect significantly the dynamics of productivity in the model.

A key aspect of the work package consists in modelling a wide array of innovation policies with the aim of exploring their impact on the economy dynamics. To this end, we differentiate between three types of innovation policies. First, standard R&D subsidies. Second, hiring scientists to conduct public R&D. Public R&D is socially desirable because it increases the productivity of private R&D. Third, hiring scientists to facilitate the adoption of new technologies by private companies. We impose a government budget constraint and consider two types of taxes, lump sum and distortionary labor income taxes.

Although our policies seem to be abstract, they are consistent with the European Innovation Policies. In fact, the European Parliament considers policies that directly target research and development which are activities to produce basic knowledge. We include this kind of policies in the model as a direct policy affecting the process of R&D creation. The government spends resources on research and development which has an explicit role in the model. Additionally, European authorities emphasize the role of industrial policy, that we consider in the model as adoption of the technologies already generated, which is also affected by a government policy. The European framework of innovation policy also highlights sectoral and education policies, which will be addressed in Work Packages 2 and 3, respectively.<sup>1</sup>

After developing our framework, we proceed to calibrate the model. We calibrate the public adoption parameters with the estimations made by WP6. The results yield some interesting take away. First, the simulations point towards the relevance of wage rigidities to the quantitative implications of the model. Second, they highlight an interesting trade off between public R&D and public diffusion. While the latter has a stronger effect on the short-run, the latter seems to have a stronger effect in the long-run.

This paper is organized as follows: section 2 describes the model; section 3 shows the response of the economy to a technology shock and evaluate the impact of considering endogenous innovation; section 4 shows the response of the economy to our fiscal policies; and section 5 concludes.

 $<sup>^1\</sup>mathrm{Source}$ : http://www.europarl.europa.eu/RegData/etudes/IDAN/2016/583778/EPRS\_IDA(2016) 583778\_EN.pdf.



## 2 Model

Our starting point is a New Keynesian DSGE model similar to Christiano et al. (2005) and Smets and Wouters (2007). We include the standard features useful for capturing the data, including: habit formation in consumption, flow investment adjustment costs, variable capital utilization and "Calvo" price and wage rigidities. In addition, monetary policy obeys a Taylor rule. We follow this approach to analyze our different policies in a context where the economy behaves close to the empirical evidence which derives realistic impulse response functions from known shocks.

The key non-standard feature is that total factor productivity depends on two endogenous variables: the creation of new technologies via R&D and the speed of adoption of these new technologies. Skilled labor is used as an input for the R&D and adoption processes. We do not model financial frictions explicitly; however, we allow for a shock that transmits through the economy like a financial shock, as we discuss below.

To study the impact of public investment in this environment, we include an active government that invests in both R&D and adoption activities. In both cases, government investment is complementary to private investment in technology. This government can also spend on goods and is financed by raising lump-sum or distortionary labor taxes.

We begin with the non-standard features of the model before briefly describing the standard ones:

## 2.1 Production Sector and Endogenous TFP: Preliminaries

In this section we describe the production sector and sketch how endogenous productivity enters the model. In a subsequent section we present the firm optimization problems.

There are two types of firms: (i) final goods producers and (ii) intermediate goods producers. There are a continuum, measure unity, of monopolistically competitive final goods producers. Each final goods firm i produces a differentiated output  $Y_t^i$ . A final good composite is then the following CES aggregate of the differentiated final goods:

$$Y_t = \left( \int_0^1 (Y_t^i)^{\frac{1}{\mu_t}} di \right)^{\mu_t} \tag{1}$$

where  $\mu_t > 1$  is given exogenously.

Each final good firm i uses  $Y_{mt}^{i}$  units of intermediate goods composite as input to produce output, according to the following simple linear technology

$$Y_t^i = Y_{mt}^i \tag{2}$$

We assume each firm sets its nominal price  $P_t^i$  on a staggered basis, as we describe later. There exists a continuum of measure  $A_t$  of monopolistically competitive intermediate goods firms that each make a differentiated product. The endogenous predetermined variable  $A_t$  is the stock of types of intermediate goods adopted in production, i.e., the stock of adopted technologies. Intermediate goods firm j produces output  $Y_{mt}^j$ . The intermediate goods composite is the following CES aggregate of individual intermediate goods:

$$Y_{mt} = \left(\int_0^{A_t} (Y_{mt}^j)^{\frac{1}{\vartheta}} dj\right)^{\vartheta} \tag{3}$$



with  $\vartheta > 1$ .

Let  $K_t^j$  be the stock of capital firm j employs,  $U_t^j$  be how intensely this capital is used, and  $L_t^j$  the stock of labor employed. Then firm j uses capital services  $U_t^j K_t^j$  and unskilled labor  $L_t^j$  as inputs to produce output  $Y_{mt}^j$  according to the following Cobb-Douglas technology:

$$Y_{mt}^{j} = \theta_t \left( U_t^{j} K_t^{j} \right)^{\alpha} (L_t^{j})^{1-\alpha} \tag{4}$$

where  $\theta_t$  is an exogenous random disturbance. As we will make clear shortly,  $\theta_t$  is the exogenous component of total factor productivity. Finally, we suppose that intermediate goods firms set prices each period. That is, intermediate goods prices are perfectly flexible, in contrast to final good prices.

Let  $\overline{Y}_t$  be average output across final goods producers. Then the production function (1) implies the following expression for the final good composite  $Y_t$ 

$$Y_t = \Omega_t \cdot \overline{Y}_t \tag{5}$$

where  $\Omega_t$  is the following measure of output dispersion

$$\Omega_t = \left( \int_0^1 (Y_t^i / \overline{Y}_t)^{\frac{1}{\mu_t}} di \right)^{\mu_t}$$

$$= 1 \text{ to a 1st order}$$
(6)

In a first order approximation,  $\Omega_t$  equals unity, implying that we can express  $Y_t$  simply as  $\overline{Y}_t$ .

Next, given the total number of final goods firms is unity, given the production function for each final goods producer (2), and given that  $Y_t$  equals  $\overline{Y}_t$ , it follows that to a first order

$$Y_t = Y_{mt} \tag{7}$$

Finally, given a symmetric equilibrium for intermediate goods (recall prices are flexible in this sector) it follows from equation (3) that we can express the aggregate production function for the finally good composite  $Y_t$  as

$$Y_t = \left[ A_t^{\vartheta - 1} \theta_t \right] \cdot (U_t K_t)^{\alpha} (L_t)^{1 - \alpha} \tag{8}$$

where the term in brackets is total factor productivity, which is the product of a term that reflects endogenous variation,  $A_t^{\vartheta-1}$ , and one that reflects exogenous variation  $\theta_t$ . Note that equation (8) holds to a first order since we impose  $\Omega_t$  equals unity.

In sum, endogenous productivity effects enter through the expansion in the variety of adopted intermediate goods, measured by  $A_t$ . We next describe the mechanisms through which new intermediate goods are created and adopted.

## 2.2 R&D and Adoption

The processes for creating and adopting new technologies are based on Comin and Gertler (2006). Let  $Z_t$  denote the stock of technologies, while as before  $A_t$  is the stock of adopted



technologies (intermediate goods). In turn, the difference  $Z_t - A_t$  is the stock of unadopted technologies. R&D expenditures increase  $Z_t$  while adoption expenditure increase  $A_t$ . We distinguish between creation and adoption because we wish to allow for realistic lags in the adoption of new technologies. We first characterize the R&D process and then turn to adoption.

#### 2.2.1 R&D: Creation of $Z_t$

There are a continuum of measure unity of innovators that use skilled labor to create new intermediate goods. Let  $L^p_{srt}$  be skilled labor employed in R&D by innovator p and let  $\varphi_t$  be the number of new technologies at time t+1 that each unit of skilled labor at t can create. We assume  $\varphi_t$  is given by

$$\varphi_t = \chi_t Z_t L_{srt}^{\rho_z - 1} L_{purt}^{\gamma_z} \tag{9}$$

where  $\chi_t$  is an exogenous disturbance to the R&D technology  $L_{purt}$  is the number of public R&D labor, and  $L_{srt}$  is the aggregate amount of skilled labor working on R&D, which an individual innovator takes as given. Following Romer (1990), the presence of  $Z_t$ , which the innovator also takes as given, reflects public learning-by-doing in the R&D process. We assume  $\rho_z < 1$  which implies that increased R&D in the aggregate reduces the efficiency of R&D at the individual level. We introduce this congestion externality so that we can have constant returns to scale in the creation of new technologies at the individual innovator level, which simplifies aggregation, but diminishing returns at the aggregate level. Our assumption of diminishing returns is consistent with the empirical evidence (see Griliches (1990)); further, with our specification the elasticity of creation of new technologies with respect to R&D becomes a parameter we can estimate, as we make clear shortly.<sup>2</sup>

The number of technologies depends also in public investment,  $L_{spurt}$ . We assume there are decreasing returns to public investment,  $\gamma_z < 1$ . All this implies that government investment in R&D apart from generating new technologies complement, or facilitates, private investment.

Let  $J_t$  be the value of an unadopted technology,  $\Lambda_{t,t+1}$  the representative household's stochastic discount factor and  $w_{st}$  the real wage for a unit of skilled labor. We can then express innovator p's decision problem as choosing  $L_{srt}^p$  to solve

$$\max_{L_{srt}^{p}} E_{t} \{ \Lambda_{t,t+1} J_{t+1} \varphi_{t} L_{srt}^{p} \} - (1 - \tau_{rt}^{s}) w_{st} L_{srt}^{p}$$
(10)

where  $\tau^s_{rt}$  is a R&D subsidy. The optimality condition for R&D is then given by

$$E_t\{\Lambda_{t,t+1}J_{t+1}\varphi_t\} - (1 - \tau_{rt}^s)w_{st} = 0$$

which implies

$$E_t\{\Lambda_{t,t+1}J_{t+1}\chi_t Z_t L_{srt}^{\rho_z - 1} L_{purt}^{\gamma_z}\} = (1 - \tau_{rt}^s) w_{st}$$
(11)

<sup>&</sup>lt;sup>2</sup>An added benefit from having diminishing returns to R&D spending is that, given our parameter estimates, steady state growth is relatively insensitive to tax policies that might affect incentives for R&D. Given the weak link between tax rates and long run growth, this feature is desirable.



The left side of equation (11) is the discounted marginal benefit from an additional unit of skilled labor, while the right side is the marginal cost.

Given that profits from intermediate goods are pro-cyclical, the value of an unadopted technology, which depends on expected future profits, will be also be pro-cyclical. This consideration, in conjunction with some stickiness in the wages of skilled labor which we introduce later, will give rise to pro-cyclical movements in  $L_{srt}$ .<sup>3</sup>

Equation (11) also describes how R&D policies stimulate innovation. Due to the existence of spillover externalities, public and private R&D are complements. After an exogenous increase in public R&D,  $L_{purt}$ , private R&D increases, because private R&D gets more productive than before. A similar effect will have a subsidy to R&D: an increase in  $\tau_{rt}^s$  stimulates R&D investment through a fall in the cost of R&D. It is important to emphasize the role of congestion externalities here. The final impact of the policies will depend on the relation between  $\rho_z$  and  $\gamma_z$ . If  $\rho_z > \gamma_z$  it's better to use subsidies to take advantage of the higher private elasticity rather than invest directly.

Finally, we allow for obsolescence of technologies.<sup>4</sup> Let  $\phi$  be the survival rate for any given technology. Then, we can express the evolution of technologies as:

$$Z_{t+1} = \varphi_t L_{srt} + \phi Z_t \tag{12}$$

where the term  $\varphi_t L_{srt}$  reflects the creation of new technologies. Combining equations (12) and (9) yields the following expression for the growth of new technologies:

$$\frac{Z_{t+1}}{Z_t} = \chi_t L_{srt}^{\rho_z} L_{purt}^{\gamma_z} + \phi \tag{13}$$

where  $\rho_z$  is the elasticity of the growth rate of technologies with respect to R&D, a parameter that we estimate.

#### **2.2.2** Adoption: From $Z_t$ to $A_t$

We next describe how newly created intermediate goods are adopted, i.e. the process of converting  $Z_t$  to  $A_t$ . Here we capture the fact that technology adoption takes time on average, but the adoption rate can vary pro-cyclically, consistent with evidence in Comin (2009). In addition, we would like to characterize the diffusion process in a way that minimizes the complications from aggregation. In particular, we would like to avoid having to keep track, for every available technology, of the fraction of firms that have and have not adopted it.

Accordingly, we proceed as follows. We suppose there are a competitive group of "adopters" who convert unadopted technologies into ones that can be used in production. They buy the rights to the technology from the innovator, at the competitive price  $J_t$ , which is the value of an adopted technology. They then convert the technology into use by employing skilled labor as input. This process takes time on average, and the conversion rate may vary endogenously.

<sup>&</sup>lt;sup>3</sup>Other approaches to motivating procyclical R&D, include introducing financial frictions Aghion et al. (2010), short term biases of innovators Barlevy (2007), or capital services in the R&D technology function Comin and Gertler (2006).

<sup>&</sup>lt;sup>4</sup>We introduce obsolescence to permit the steady state share of spending on R&D to match the data.



In particular, the pace of adoption depends positively on the level of adoption expenditures in the following simple way: an adopter succeeds in making a product usable in any given period with probability  $\lambda_t$ , which is an increasing and concave function of the amount of skilled labor employed,  $L_{sat}$ , and  $L_{puat}$  is the amount of skilled public R&D workers used in the adoption of the technology:

$$\lambda_t = \bar{\lambda}_0 * (Z_t L_{sat})^{\rho_{\lambda}} * \left(1 + \bar{\lambda}_{pu} * (Z_t L_{puat})^{\rho_{\lambda_{pu}}}\right)$$
(14)

with  $\rho_{\lambda}$ ,  $\rho_{\lambda pu} \in (0,1)$  and  $(\bar{\lambda}_0, \bar{\lambda}_{pu}) > 0$ . We augment  $L_{sat}$  by a spillover effect from the total stock of technologies  $Z_t$  - think of the adoption process as becoming more efficient as the technological state of the economy improves. The practical need for this spillover is that it ensures a balanced growth path: as technologies grow, the number of new goods requiring adoption increases, but the supply of labor remains unchanged. Hence, the adoption process must become more efficient as the number of technologies expands. Unlike the specification used for R&D, there is no separate shock to the productivity of adoption activities in (14). We are constrained to introduce this asymmetry because we do not have a direct observable to measure adoption labor or  $\lambda_t$ . The identified series of adoption hours,  $L_{sat}$ , can be interpreted as the effective number of adoption hours.

Our adoption process implies that technology diffusion takes time on average, consistent with the evidence. If  $\lambda$  is the steady state value of  $\lambda_t$ , then the average time it takes for a new technology be adopted is  $1/\lambda$ . Away from the steady state, the pace of adoption will vary with skilled input  $L_{sat}$ . We turn next to how  $L_{sat}$  is determined.

Once in usable form, the adopter sells the rights to the technology to a monopolistically competitive intermediate goods producer that makes the new product using the production function described by equation (8). Let  $\Pi_{mt}$  be the profits that the intermediate goods firm makes from producing the good, which arise from monopolistically competitive pricing. The adopter sells the new technology at the competitive price  $V_t$ , which is the present discounted value of profits from producing the good, given by

$$V_t = \Pi_{mt} + \phi E_t \{ \Lambda_{t,t+1} V_{t+1} \}$$
 (15)

Then we may express the adopter's maximization problem as choosing  $L_{sat}$  to maximize the value  $J_t$  of an unadopted technology, given by

$$J_t = \max_{L_{sat}} E_t \{ -(1 - \tau_{at}^s) w_{st} L_{sat} + \phi \Lambda_{t,t+1} [\lambda_t V_{t+1} + (1 - \lambda_t) J_{t+1} \}$$
 (16)

subject to equation (14). The first term in the Bellman equation reflects total adoption expenditures that considers a subsidy to technological adoption  $\tau_{at}^s$ , while the second is the discounted benefit: the probability weighted sum of the values of adopted and unadopted technologies.

The first order condition for  $L_{sat}$  is

$$\lambda_t' \cdot \phi E_t \{ \Lambda_{t,t+1} [V_{t+1} - J_{t+1}] \} = (1 - \tau_{at}^s) w_{st}$$
 (17)

The term on the left is the marginal gain from adoption expenditures: the increase in the adoption probability  $\lambda_t$  times the discounted difference between an adopted versus unadopted technology. The right side is the marginal cost.



The term  $V_t - J_t$  is pro-cyclical, given the greater influence of near term profits on the value of adopted technologies relative to unadopted ones. Given this consideration and the stickiness in  $w_{st}$  which we alluded to earlier,  $L_{sat}$  varies pro-cyclically. The net implication is that the pace of adoption, given by  $\lambda_t$ , will also vary pro-cyclically.

The effect of public adoption is through  $\lambda'$  that increases when  $L_{spuat}$  goes up. This also implies that  $L_{sat}$  rises for the same reasons it increases with  $[V_{t+1} - J_{t+1}]$ . Adoption subsidies have similar effects and the difference between innovating directly and subsidizing it depends on the difference between  $\rho_{\lambda}$  and  $\rho_{\lambda pu}$ . We analyze this extensively in the results section.

Given that  $\lambda_t$  does not depend on adopter-specific characteristics, we can sum across adopters to obtain the following relation for the evolution of adopted technologies

$$A_{t+1} = \lambda_t \phi [Z_t - A_t] + \phi A_t \tag{18}$$

where  $Z_t - A_t$  is the stock of unadopted technologies.

#### 2.3 Households

The representative household consumes and saves in the form of capital and riskless bonds which are in zero net supply. It rents capital to intermediate goods firms. As in the standard DSGE model, there is habit formation in consumption. Also as is standard in DSGE models with wage rigidity, the household is a monopolistically competitive supplier of differentiated types of labor.

The household's problem differs from the standard setup in two ways. First it supplies two types of labor: unskilled labor  $L_t^h$  which is used in the production of intermediate goods and skilled labor which is used either for R&D or adoption,  $L_{st}^h$ .

Second, we suppose that the household has a preference for the safe asset, which we motivate loosely as a preference for liquidity and capture by incorporating bonds in the utility function, following Krishnamurthy and Vissing-Jorgensen (2012). Further, following Fisher (2015), we introduce a shock to liquidity demand  $\varrho_t > 0$ . As we show, the liquidity demand shock transmits through the economy like a financial shock. It is mainly for this reason that we make use of it, as opposed to a shock to the discount factor.<sup>5</sup>

Let  $C_t$  be consumption,  $B_t$  holdings of the riskless bond,  $\Pi_t$  profits from ownership of monopolistically competitive firms,  $K_t$  capital,  $Q_t$  the price of capital,  $R_{kt}$  the rate of return, and  $D_t$  the rental rate of capital. Then the households' decision problem is given by

$$\max_{C_{t}, B_{t+1}, L_{t}^{h}, L_{st}^{h}, K_{t+1}} E_{t} \sum_{\tau=0}^{\infty} \beta^{\tau} \left\{ \log(C_{t+\tau} - bC_{t+\tau-1}) + \varrho_{t} B_{t+1} - \left[ \frac{\upsilon(L_{t}^{h})^{1+\varphi} + \upsilon_{s}(L_{st}^{h})^{1+\varphi}}{1+\varphi} \right] \right\}$$
(19)

subject to

$$C_t = (1 - \tau_t^l) \left[ w_t^h L_t^h + w_{st}^h L_{st}^h \right] + \Pi_t + R_{kt} Q_{t-1} K_t - Q_t K_{t+1} + R_t B_t - B_{t+1} + T_t$$
 (20)

<sup>&</sup>lt;sup>5</sup>Another consideration is that the liquidity demand shock induces positive co-movement between consumption and investment, while that is not always the case for a discount factor shock.



with

$$R_{kt} = \frac{D_t + Q_t}{Q_{t-1}} \tag{21}$$

 $\Lambda_{t,t+1}$ , the household's stochastic discount factor, is given by

$$\Lambda_{t,t+1} \equiv \beta u'(C_{t+1})/u'(C_t) \tag{22}$$

where  $u'(C_t) = 1/(C_t - bC_{t-1}) - b/(C_{t+1} - bC_t)$ . In addition, let  $\zeta_t$  be the liquidity preference shock in units of the consumption good:

$$\zeta_t = \varrho_t / u'(C_t) \tag{23}$$

Then we can express the first order necessary conditions for capital and the riskless bond as, respectively:

$$1 = E_t \{ \Lambda_{t,t+1} R_{kt+1} \} \tag{24}$$

$$1 = E_t \{ \Lambda_{t,t+1} R_{t+1} \} + \zeta_t \tag{25}$$

As equation (25) indicates, the liquidity demand shock distorts the first order condition for the riskless bond. A rise in  $\zeta_t$  acts like an increase in risk: given the riskless rate  $R_{t+1}$  the increase in  $\zeta_t$  induces a precautionary saving effect, as households reduce current consumption in order to satisfy the first order condition (which requires a drop in  $\Lambda_{t,t+1}$ ). It also leads to a drop in investment demand, as the decline in  $\Lambda_{t,t+1}$  raises the required return on capital, as equation (24) implies. The decline in the discount factor also induces a drop in R&D and investment.

Overall, the shock to  $\zeta_t$  generates positive co-movement between consumption and investment similar to that arising from a monetary shock. To see, combine equations (24) and (25) to obtain

$$E_t\{\Lambda_{t,t+1}(R_{kt+1} - R_{t+1})\} = \zeta_t \tag{26}$$

To a first order an increase in  $\zeta_t$  has an effect on both  $R_{kt+1}$  and  $\Lambda_{t,t+1}$  that is qualitatively similar to that arising from an increase in  $R_{t+1}$ . In addition, note that an increase in  $\zeta_t$  raises the spread  $R_{kt+1} - R_{t+1}$ . In this respect it transmits through the economy like a financial shock. Indeed, we show later that our identified liquidity demand shock is highly correlated with credit spreads.

Since it is fairly conventional, we defer until later a description of the household's wage-setting and labor supply behavior.

#### 2.4 Firms

#### 2.4.1 Intermediate goods firms: factor demands

Given the CES function for the intermediate good composite (3), in the symmetric equilibrium each of the monopolistically competitive intermediate goods firms charges the markup  $\vartheta$ . Let  $p_{mt}$  be the relative price of the intermediate goods composite. Then from



(3) and the production function (4), cost minimization by each intermediate goods producer yields the following standard first order conditions for capital, capital utilization, and unskilled labor:

$$\alpha \frac{p_{mt}Y_{mt}}{K_t} = \vartheta[D_t + \delta(U_t)Q_t] \tag{27}$$

$$\alpha \frac{p_{mt} Y_{mt}}{U_t} = \vartheta \delta'(U) Q_t K_t \tag{28}$$

$$(1 - \alpha)\frac{p_{mt}Y_{mt}}{L_t} = \vartheta w_t \tag{29}$$

#### 2.4.2 Final goods producers: price setting

Let  $P_t^i$  be the nominal price of final good i and  $P_t$  the nominal price level. Given the CES relation for the final good composite, equation (1), the demand curve facing each final good producer is:

$$Y_t^i = \left(\frac{P_t^i}{P_t}\right)^{-\mu_t/(\mu_t - 1)} Y_t \tag{30}$$

where the price index is given by:

$$P_t = \left(\int_0^1 (P_t^i)^{-1/(\mu_t - 1)} di\right)^{-(\mu_t - 1)},\tag{31}$$

Following Smets and Wouters (2007), we assume Calvo pricing with flexible indexing. Let  $1 - \xi_p$  be the i.i.d probability that a firm is able to re-optimize its price and let  $\pi_t = P_t/P_{t-1}$  be the inflation rate. Firms that are unable to re-optimize during the period adjust their price according to the following indexing rule:

$$P_t^i = P_{t-1}^i \pi_{t-1}^{\iota_p} \pi^{1-\iota_p} \tag{32}$$

where  $\pi$  is the steady state inflation rate and  $\iota_p$  reflects the degree of indexing to lagged inflation.

For firms able to re-optimize, the optimization problem is to choose a new reset price  $P_t^*$  to maximize expected discounted profits until the next re-optimization, given by

$$E_t \sum_{\tau=0}^{\infty} \xi_p^{\tau} \Lambda_{t,t+\tau} \left( \frac{P_t^* \Gamma_{t,t+\tau}}{P_{t+\tau}} - p_{mt+\tau} \right) Y_{t+\tau}^i$$
(33)

subject to the demand function (30) and where

$$\Gamma_{t,t+\tau} \equiv \prod_{k=1}^{\tau} \pi_{t+k-1}^{\iota_p} \pi^{1-\iota_p} \tag{34}$$

The first order condition for  $P_t^*$  and the price index that relates  $P_t$  to  $P_t^*, P_{t-1}$  and  $\pi_{t-1}$  are then respectively:



$$0 = E_t \sum_{\tau=0}^{\infty} \xi_p^{\tau} \Lambda_{t,t+\tau} \left[ \frac{P_t^* \Gamma_{t,t+\tau}}{P_{t+\tau}} - \mu_{t+\tau} p_{mt+\tau} \right] Y_{t+\tau}^i$$
 (35)

$$P_{t} = \left[ (1 - \xi_{p}) (P_{t}^{*})^{-1/(\mu_{t} - 1)} + \xi_{p} \left( \pi_{t-1}^{\iota_{p}} \pi^{1 - \iota_{p}} P_{t-1} \right)^{-1/(\mu_{t} - 1)} \right]^{-(\mu_{t} - 1)}$$
(36)

Equations (35) and (36) jointly determine inflation. In the loglinear equilibrium, current inflation is a function of current real marginal cost  $p_{mt}$ , expected future inflation, and lagged inflation.

#### 2.4.3 Capital producers: investment

Competitive capital producers use final output to make new capital goods, which they sell to households, who in turn rent the capital to firms. Let  $I_t$  be new capital produced and  $p_{kt}$  the relative price of converting a unit of investment expenditures into new capital (the replacement price of capital), and  $\gamma_y$  the steady state growth in  $I_t$ . In addition, following Christiano et al. (2005), we assume flow adjustment costs of investment. The capital producers' decision problem is to choose  $I_t$  to solve

$$\max_{I_t} E_t \sum_{\tau=0}^{\infty} \Lambda_{t,t+\tau} \left\{ Q_{t+\tau} I_{t+\tau} - p_{kt+\tau} \left[ 1 + f \left( \frac{I_{t+\tau}}{(1+\gamma_y)I_{t+\tau-1}} \right) \right] I_{t+\tau} \right\}$$
(37)

where the adjustment cost function is increasing and concave, with f(1) = f'(1) = 0 and f''(1) > 0. We assume that  $p_{kt}$  follows an exogenous stochastic process.

The first order condition for  $I_t$  the relates the ratio of the market value of capital to the replacement price (i.e. "Tobin's Q") to investment, as follows:

$$\frac{Q_t}{p_{kt}} = 1 + f\left(\frac{I_t}{(1+\gamma_y)I_{t-1}}\right) + \frac{I_t}{(1+\gamma_y)I_{t-1}}f'\left(\frac{I_t}{(1+\gamma_y)I_{t-1}}\right) - E_t\Lambda_{t,t+1}\left(\frac{I_{t+1}}{(1+\gamma_y)I_t}\right)^2 f'\left(\frac{I_{t+1}}{(1+\gamma_y)I_t}\right)$$
(38)

#### 2.4.4 Employment agencies and wage adjustment

As we noted earlier, the household is a monopolistically competitive supplier of labor. Think of the household as supplying its labor to form a labor composite. Firms then hire the labor composite. The only difference from the standard DSGE model with wage rigidity, is that households now supply two types of labor, skilled and unskilled. It also sets wages for each type.

Let  $X_t = \{L_t, L_{st}\}$  denote a labor composite. As is standard, we assume that  $X_t$  is the following CES aggregate of the differentiated types of labor that households provide:

$$X_{t} = \left[ \int_{0}^{1} X_{t}^{h \frac{1}{\mu_{wt}}} dh \right]^{\mu_{wt}}. \tag{39}$$

where  $\mu_{wt} > 1$  obeys an exogenous stochastic process<sup>6</sup>.

<sup>&</sup>lt;sup>6</sup>In estimating the model we introduce wage markup shocks to the wage setting problem of unskilled labor only, so the markup for skilled labor is constant at its steady state level.



Let  $W_{xt}$  denote the wage of the labor composite and let  $W_{xt}^h$  be the nominal wage for labor supplied of type x by household h. Then profit maximization by competitive employment agencies yields the following demand for type x labor:

$$X_t^h = \left(\frac{W_{xt}^h}{W_{xt}}\right)^{-\mu_{wt}/(\mu_{wt}-1)} X_t, \tag{40}$$

with

$$W_{xt} = \left[ \int_0^1 W_{xt}^{h - \frac{1}{\mu_{wt} - 1}} dh \right]^{-(\mu_{wt} - 1)}.$$
 (41)

As with price setting by final goods firms, we assume that households engage in Calvo wage setting with indexation. Each period a fraction  $1 - \xi_w$  of households re-optimize their wage for each type. Households who are not able to re-optimize adjust the wage for each labor type according to the following indexing rule:

$$W_{xt}^{h} = W_{xt-1}^{h} \pi_{t-1}^{\iota_w} \pi^{1-\iota_w} \gamma. \tag{42}$$

where  $\gamma$  is the steady state growth rate of labor productivity.

The remaining fraction of households choose an optimal reset wage  $W_{xt}^*$  by maximizing

$$E_{t} \left\{ \sum_{\tau=0}^{\infty} \xi_{w}^{\tau} \beta^{\tau} \left[ u'(C_{t+\tau}) \frac{(1-\tau_{t+\tau}^{l}) W_{xt}^{*} \Gamma_{wt,t+\tau}}{P_{t+\tau}} X_{t+\tau}^{h} - \upsilon \frac{X_{t+\tau}^{h-1+\varphi}}{1+\varphi} \right] \right\}$$
(43)

subject to the demand for type h labor and where the indexing factor  $\Gamma_{xt,t+\tau}$  is given by

$$\Gamma_{wt,t+\tau} \equiv \prod_{k=1}^{\tau} \pi_{t+k-1}^{\iota_w} \pi^{1-\iota_w} \gamma \tag{44}$$

The first order condition for the re-set wage and the equation for the composite wage index as a function of the reset wage, inflation and the lagged wage are given, respectively, by

$$E_t \left\{ \sum_{\tau=0}^{\infty} \xi_w^{\tau} \Lambda_{t,\tau} \left[ \frac{(1-\tau_{t+\tau}^l) W_{xt}^* \Gamma_{wt,t+\tau}}{P_{t+\tau}} - \mu_{wt} \upsilon \frac{X_{t+\tau}^h \varphi}{u'(C_{t+\tau})} \right] X_{t+\tau}^h \right\} = 0 \tag{45}$$

$$W_{xt} = \left[ (1 - \xi_w) (W_{xt}^*)^{-1/(\mu_{wt} - 1)} + \xi_p \left( \gamma \pi_{t-1}^{\iota_w} \pi^{1 - \iota_w} W_{xt-1} \right)^{-1/(\mu_{wt} - 1)} \right]^{-(\mu_{wt} - 1)}$$
(46)

#### 2.4.5 Fiscal and monetary policy

We take two approaches when including government, lump-sum or distortionary taxes. If we assume that government activities  $G_t$ ,  $L_{purt}$ ,  $L_{puat}$ ,  $\kappa_{rt}$ , and  $\kappa_{at}$  are financed with lump sum taxes  $T_t$ , government's budget constraint is

$$G_t + w_{st}(L_{purt} + L_{puat}) + w_{st}(\tau_{rt}^s L_{srt} + \tau_{at}^s L_{sat}) = T_t$$

$$\tag{47}$$



while with distortionary taxes it writes

$$G_t + w_{st}(L_{purt} + L_{puat}) + w_{st}(\tau_{rt}^s L_{srt} + \tau_{at}^s L_{sat}) = \tau_t^l(w_t L_t + w_{st} L_{st})$$
(48)

Further, the (log) deviation of  $G_t$ ,  $L_{purt}$ ,  $L_{puat}$ ,  $\tau_{rt}^s$ , and  $\tau_{at}^s$  from the deterministic trend of the economy follows AR(1) processes. Formally, for each  $\mathcal{X}_t \in \{G_t, L_{purt}, L_{puat}, \tau_{rt}^s, \tau_{at}^s\}$ , we have

$$\log(\mathcal{X}_t/(1+\gamma_u)^t) = (1-\rho_{\mathcal{X}})\bar{\mathcal{X}} + \rho_{\mathcal{X}}\log(\mathcal{X}_{t-1}/(1+\gamma_u)^{t-1}) + \epsilon_t^{\mathcal{X}}$$
(49)

Next, we suppose that monetary policy obeys a Taylor rule. Let  $R_{nt+1}$  denote the gross nominal interest rate,  $R_n$  the steady state nominal rate,  $\pi^0$  the target rate of inflation,  $L_t$  total employment and  $L^{ss}$  steady state employment. The (nonlinear) Taylor rule for monetary policy that we consider is given by

$$R_{nt+1} = \left[ \left( \frac{\pi_t}{\pi^0} \right)^{\phi_\pi} \left( \frac{L_t}{L^{ss}} \right)^{\phi_y} R_n \right]^{1-\rho} \cdot R_{nt}^{\rho} \tag{50}$$

where the relation between the nominal and real rate is given by the Fisher relation:

$$R_{nt+1} = R_{t+1} \cdot \pi_{t+1} \tag{51}$$

and where  $\phi_{\pi}$  and  $\phi_{y}$  are the feedback coefficients on the inflation gap and capacity utilization gap respectively. We use the employment gap to measure capacity utilization as opposed to an output gap for two reasons. First, Takahashi et al. (2016) show that measures of employment are the strongest predictors of changes in the Fed Funds rate. Second, along these lines, the estimates of the Taylor rule with the employment gap appear to deliver a more reasonable response of the nominal rate to real activity within this model than does one with an output gap.<sup>7</sup>

In addition, we impose the zero lower bound constraint on the net nominal interest rate, which implies that the gross nominal rate cannot fall below unity.

$$R_{nt+1} > 1 \tag{52}$$

#### 2.5 Resource constraints and equilibrium

The resource constraint is given by

$$Y_{t} = C_{t} + p_{kt} \left[ 1 + f \left( \frac{I_{t+\tau}}{(1+\gamma_{u})I_{t+\tau-1}} \right) \right] I_{t} + G_{t}$$
 (53)

Capital evolves according to

$$K_{t+1} = I_t + (1 - \delta(U_t))K_t \tag{54}$$

<sup>&</sup>lt;sup>7</sup>Part of the problem may be that the behavior of the flexible price equilibrium output is quite complex in the model, particularly given the endogenous growth sector. As a robustness check on our specification of the Taylor rule, we estimate a version of the model in which we adjust the employment gap for demographic effects on the size of the labor force; our estimation results are robust to this change.

## Innovation Policies and Growth



The market for skilled labor must clear:

$$L_{st} = (Z_t - A_t) * (L_{sat} + L_{puat}) + L_{srt} + L_{purt}$$
(55)

Finally, the market for risk-free bonds must clear, which implies that in equilibrium, risk-free bonds are in zero net supply

$$B_t = 0$$

This completes the description of the model.

#### 2.6 Calibration

We take the calibration of the basic parameters from Anzoategui et al. (2015), shown in Table (4). Some of these parameters are from the standard RBC literature. For representative agent, closed economies this is a natural starting point.

However, we calibrate the technology parameters for the European Union, and specially UK, as follows. The elasticity of  $\lambda$  to private adoption activities  $\rho_{\lambda}$  is set to 0.95 and  $\rho_{\lambda_{pu}}$  to 0.7.  $\bar{\lambda}$  is set to produce an average adoption lag of 7 years. The obsolescence rate  $(1 - \phi)$  is to 8% yearly. We use the estimates of WP6 to calibrate the parameters in  $\varphi_t$ . The private technological parameter  $\rho_z$  is set to 0.38 and the public technological elasticity to 0.29. Table (5) describes the calibration of the parameters for the stochastic processes that we take from the estimates given in Anzoategui et al. (2015). Table (6) shows the calibration of the parameters of the fiscal policy.



# Innovation Policies and Growth

Parameter	Description	Value
$\alpha$	Capital share	1/3
δ	Capital depreciation	0.02
$\beta$	Discount factor	0.995
$\varphi$	Inv. Frisch elasticity	3.381
$rac{arphi}{rac{G}{Y}}$	SS govt. consumption/output	0.2
$\dot{\gamma}_y$	SS output growth	1.87%
$\mu$	SS final goods mark-up	1.1
$\mu_w$	SS wage mark-up	1.87%
$\vartheta$	Intermediate goods mark-up	1.35
$1-\phi$	Obsolescence rate	0.08/4
$\overline{\lambda}$	SS adoption lag	0.15/4
$ ho_{\lambda}$	Private adoption elasticity	0.95
$ ho_z$	Private R&D elasticity	0.38
$\rho$	Taylor rule smoothing	0.805
$\phi_{\pi}$	Taylor rule inflation	1.571
$\phi_y$	Taylor rule labor	0.47
f''	Investment adj. cost	1.386
$ \begin{array}{c} \phi_y \\ f'' \\ \frac{\delta'(U)}{\delta} \\ \xi_p \\ \xi_w \end{array} $	Capital utiliz. Elast.	3.868
$\xi_p$	Calvo prices	0.927
$\dot{\xi_w}$	Calvo wages	0.87
$\iota_p$	Price indexation	0.276
$\iota_w$	Wage indexation	0.338
b	Consumption habit	0.389

Table 4: Calibration.



Parameter	Description	Value
$\rho_{\theta}$	TFP	0.91
$ ho_{pk}$	Investment	0.87
$ ho_{arrho}$	Liquidity demand	0.91
$ ho_{mp}$	Monetary	0.57
$ ho_{\mu}$	Mark-up	0.38
$ ho_g$	Govt. expenditures	0.99
$ ho_{\mu_w}$	Wage mark-up	0.26
$ ho_\chi$	R&D	0.84
$\sigma_{\theta}$	TFP	0.51
$\sigma_{pk}$	Investment	0.74
$\sigma_{\varrho}$	Liquidity demand	0.23
$\sigma_{mp}$	Monetary	0.1
$\sigma_{\mu}$	Mark-up	0.1
$\sigma_g$	Govt. expenditures	2.87
$\sigma_{\mu_w}$	Wage mark-up	0.3
$\sigma_{\chi}$	R&D	2.13

Table 5: Calibration of stochastic processes.

Parameter	Description	Value
$\overline{\lambda}_{pu}$	SS public adoption lag	0.2
$ ho_{\lambda_{pu}}$	Public adoption elasticity	0.7
$\gamma_z$	Public R&D elasticity	0.29
$ ho_{lr}$	Persistence in Pub Inv in Adoption	0.9
$ ho_{la}$	Persistence in Pub Inv in R&D	0.9
$ ho_{\kappa_r}$	Persistence Pub subsidies in Adoption	0.9
$ ho_{\kappa_a}$	Persistence Pub subsidies in R&D	0.9
$\sigma_{lr}$	Pub Inv in Adoption	0.01
$\sigma_{la}$	Pub Inv in R&D	0.01
$\sigma_{\kappa_r}$	Pub subsidies in Adoption	0.01
$\sigma_{\kappa_a}$	Pub subsidies in R&D	0.01
G/Earnings	SS gov spending share	0.8
$L_{spua}/Earnings$	SS adoption inv share	0.05
$L_{spur}/Earnings$	SS R&D inv share	0.05
$\kappa_a/Earnings$	SS adoption subsidy share	0.05
$\kappa_r/Earnings$	SS R&D subsidy share	0.05

Table 6: Calibration of government parameters.



## 3 The effect of Aggregate Shocks

Figure (1) depicts the IRF for a one standard deviation of a monetary shock and a conventional TFP shock. Our results resemble the results on Anzoategui et al. (2015) and Comin and Gertler (2006). First, the economy with endogenous technology is more volatile than without it. The last is true for both monetary and TFP shocks. Second, all the responses—in this case to demand and supply shocks— are more persistent with endogenous technology.

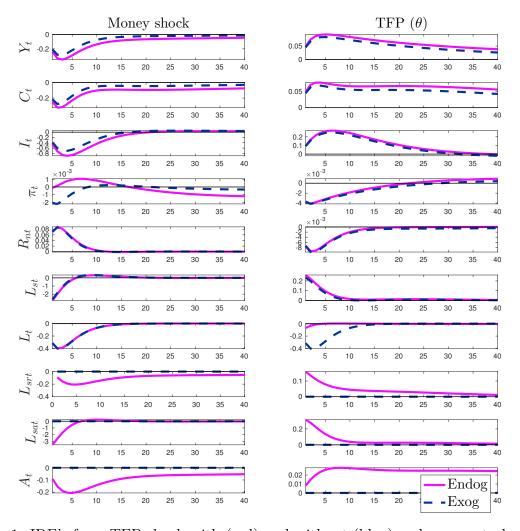


Figure 1: IRF's for a TFP shock with (red) and without (blue) endogenous technology.

Finally, it is worth to notice a key feature of our model: R&D and diffusion investment are both procyclical; the responses of  $L_{sat}$  and  $L_{srt}$  follow the response of GDP. The implication of this is that adoption of technology is procyclical as well. When there is a positive shock to the exogenous technological factor, adoption  $A_t$  (the second component of the aggregate TFP). As a result, total TFP increases endogenously. In particular, the growth rate of TFP expands/declines transitorily causing a permanent impact on the level of TFP.



## 4 The effect of government investment in R&D

In this section, we show the response of the economy to government spending on investment in R&D and Adoption. In the following, we analyze two cases: first, we assume that government finance spending with lump-sum taxes, and second, with distortionary labor taxes as described in the exposition of the model.

## 4.1 Lump-sum taxes

Figures (2) and (3) show the IRF's for a one standard deviation diffusion (left), R&D (center), and in R&D subsidies (right) for a government that finances its activities with lump-sum taxes. To show the relevance of the different elasticities for our different policies, we consider two alternative calibrations. First, we take the benchmark calibration (blue dashed line). Second, we show a case with high elasticity of adoption and R&D to public investment (pink solid line). In the latter, public investment impact on  $\lambda_t$  and  $\varphi_t$  is equivalent to the impact of private activities. Recall that in the baseline calibration, the government is less efficient in both the probability of adopting a new technology  $\lambda_t$  and in the productivity of R&D  $\varphi_t$ .



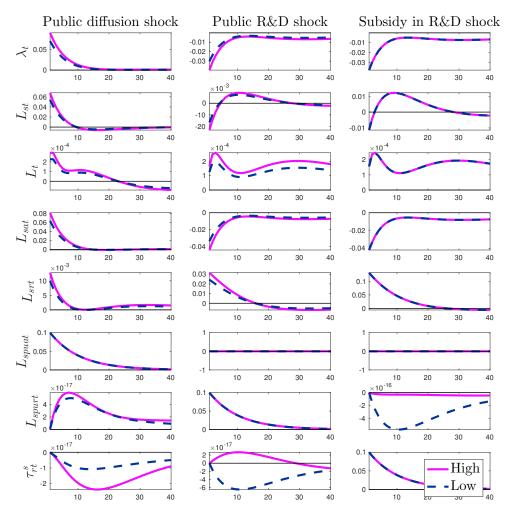


Figure 2: IRF's for shocks to public investment with lump-sum taxes. Pink-solid: high elasticities of government investment in innovation. Blue-dashed: baseline.

Figure (2) suggests that first-order effects happen mainly through labor markets. As in this model investment in technology is made with skilled labor, government activities push skilled labor markets by demanding a higher quantity of skilled labor, and hence pushing wages up (see Figure (3)). The increase in wages is slow due to the wage rigidities. Left panel of Figure (2) shows an increase in public adoption  $L_{puat}$ . After a shock to  $L_{puat}$ , skilled wages also go up, so households start supplying more skilled labor overall.

This additional labor supply has to be distributed among the different private activities. This increases why both private investment in adoption,  $L_{sat}$ , and private R&D investment,  $L_{srt}$ , constituting a spillover from public to private activities. Also, there is an increase in unskilled labor, that is due to the–expected– increase in aggregate productivity and investment, which raises unskilled wages. Hence, as a result of the combination of the increase in investment, productivity, and labor, GDP increases immediately and persistently. Consumption sustains this growth as wages and firm's earnings soar. This is the contribution of public investment to medium-term business cycles.

However, investment in R&D doesn't have the same effect of adoption activities. Center panels of Figures (2) and (3) show the IRF's to a one standard deviation of public



R&D investment,  $L_{purt}$ . Recall that R&D activities don't translate to productivity immediately, it is adoption which does the job of materializing ideas into goods. That is why there are huge differences between the two cases.

When public R&D increases, agents know that the level of technology will be higher in the medium term. As a result, they want to consume more because, they are wealthier. This reaction triggers an increase in interest rates which lowers the value of adopted technologies. As a result, adoption declines upon impact. R&D instead increases because public R&D enhances the productivity of private R&D. Hence the different evolution private R&D and adoption investments.

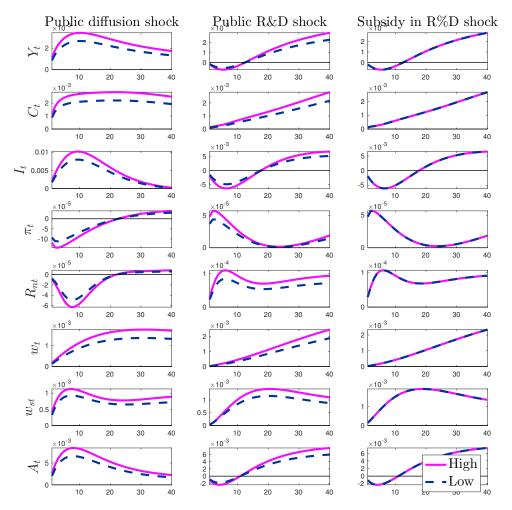


Figure 3: IRF's for shocks to public investment with lump-sum taxes. Pink-solid: high elasticities of government investment in innovation. Blue-dashed: baseline.

Finally, the right panel of Figures (2) and (3) show the response of the economy to an innovation subsidy shock. An important feature of innovation subsidies is that they can take advantage of the different impacts public and private investment have. In our baseline calibration, government investment in innovation has a lower elasticity, so it would be optimal to raise—lump-sum— taxes and then subsidy private innovation activities instead of spending directly on innovation.



Figures (2) and (3) show that a shock to R&D subsidy, in our calibration, resembles the response of the economy to R%D as if public investment was in the case of high elasticities. This means that the raise in subsidy is enough to induce high investment in R&D and take advantage of the higher productivity the private activities have. The only difference would be the responses of labor markets. As these shocks are transmitted through private demand of labor we see that  $L_{srt}$  expands largely than the case of the shock to public R&D, and its impact on the rest of the labor variables is essentially the same. An interesting result is that for our calibration a subsidy will impact  $\lambda_t$  in the same size than investment in R&D, which implies that the response on diffusion  $A_t$  is the same than in the high case. Additionally, GDP and consumption follow the response of  $A_t$  in the high case.

In summary, a subsidy or tax to innovation will be more useful when the differences in decreasing returns of public and private investment are higher an the latter is bigger than the former. This also implies that having accurate estimates of these elasticities is key in order to evaluate the impact of the different possible policies governments can undertake in order to generate sustained growth.

## 4.2 The effect on returns and the skill premium

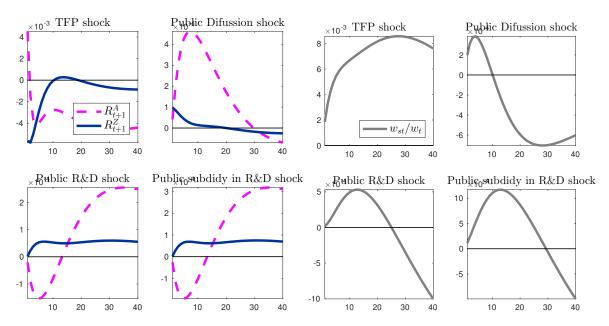


Figure 4: The effect of policies on returns to technology (four left panels) and on the skill premium (four right panels).

Since in this economy there are many agents that have different roles, it is useful to analyze the effect of shocks on the returns of the different activities. For the one side, we analyze the effect of our policies on the return to R&D and Adoption. These returns are computed as follows:

$$E_{t}\left[\Lambda_{t+1}R_{t+1}^{A}\right] = E_{t}\left[\Lambda_{t+1}\phi\frac{V_{t+1}}{V_{t} - \pi_{t}}\right] = 1 \text{ and } E_{t}\left[\Lambda_{t+1}R_{t+1}^{Z}\right] = E_{t}\left[\Lambda_{t+1}\frac{J_{t+1}\varphi_{t}}{(1 - \tau_{rt}^{s})w_{st}}\right] = 1.$$



By the other hand, we compute the inequality our policies generate on workers, which is the skill premium  $w_{st}/w_t$ .

Figure (4) shows the response of returns and the skill premium to a TFP shock and also to our policies. The four left panels show  $R_{t+1}^A$  and  $R_{t+1}^Z$ , while the four right left panels show the skill premium. Unsurprisingly, direct investment in diffusion and R&D increase their respective returns. This is because of the complementarity between public and private activities. Through the returns, we can understand the differences between investing in R&D and adoption. The return to adoption is much more volatile (for any shock), this is because they are more exposed to short- and medium-run fluctuations, while the return to R&D only reacts some periods after the policy. This is due to the adoption lag. In the first periods after the policy, there are no incentives to invest in R&D privately. However, the final effect is positive and highly persistent in the medium term as technologies become profitable.

The skill premium also responds strongly to our policies. In fact, all these policies, even with lump-sum taxes generate inequality in the short-run. This is more pronounced for R&D policies because of the adoption lag. Surprisingly, the subsidy has a longer effect on inequality, that may be due to the higher impact of this policy on  $Z_t$ . However, all our policies impact the skill premium negatively generating more equality in the long-run.

## 4.3 Distortionary taxation and the role of wage rigidities

In this section we explore the impact of wage rigidities and how they determine the effect of our policies. We do this to show that the way government is financed matters, but in our setup it is camouflaged by this feature. The fact that we are taxing only labor in order to finance or subsidy skilled labor demand turns rigidities to be key in our results.

In what follows, we study the effects of innovation policies financed with distortionary taxation, but we set the probability of not adjusting wages to be 75% lower than in the baseline calibration and maintain the rest of the parameters fixed. Figures (5) and (6) show this case. The pink solid line shows the response of the economy with distortionary taxes and the blue dashed with lump-sum (that is, essentially, the baseline calibration).

Now the joint role of distortionary taxes and wage rigidities appears, and it seems to be important. In this case, our policies trigger an increase in taxes, but the dynamics of the economy differ greatly between the two ways of financing, as expected. This, because in a low rigidity case, wages respond significantly to labor taxes not as with high rigidities. Hence, both the supply of labor and consumption will be altered respect to the baseline situation, inducing differences between distortionary and non distortionary taxation.

Two forces now affect labor dynamics if government investment is financed with distortionary taxes. By the one side, our three policies demand skilled labor; by the other, taxes must increase in order to finance these policies, which distorts the labor supply of both types of labor. These two forces are present only in skilled labor after a shock to any of our policies, implying that its effects on skilled labor will be ambiguous. However, on impact, unskilled labor should decrease due to the raise in labor tax rates, while there is not an exogenous force demanding more unskilled labor. This happens in the short term, but while adoption of technology takes place, labor recovers. Hence, it follows that the



response of labor depends on the response of labor taxes: the higher the latter increases, the lower labor falls. Thing that takes place after a shock to any of our three policies, with a significant impact on the real economy.

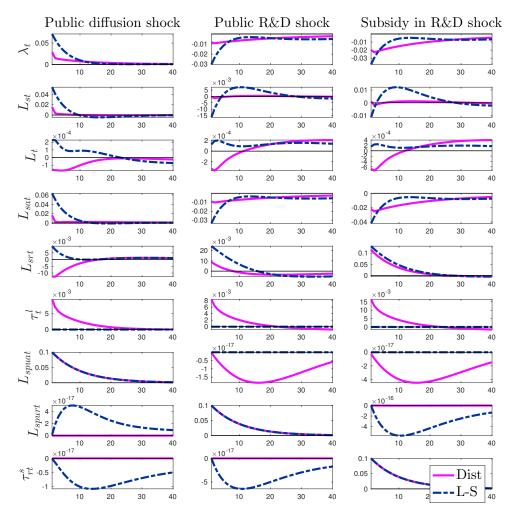


Figure 5: IRF's for shocks to public investment with distortionary taxes and low rigidities  $(\xi_w^* = 0.25\xi_w)$ . Pink solid: distorsionary labor taxes. Blue dashed: lump-sum taxes.

Moreover, the response of the real economy is very different as well. In the case of a shock to diffusion, GDP and consumption reach a maximum that is a third of the lump-sum case. This is because rigidities keep labor costs constant relative to the low case so the economy experiences an accentuated boom that follows the development of labor markets and the expansion of adoption. In the medium term the expansion of GDP and consumption is determined by the effect of distortionary taxes, seeing a lower increase than when spending is financed with lump-sum taxes. For the case of our R&D policies, the pattern is similar. A subsidy calls for a bigger increase in taxes, which dampen the effect of subsidy policies, as can be seen by the stronger negative response of consumption and GDP than the case of lump-sum taxes and in public R&D. Actually, with distortionary taxation it would be better to use pubic R&D than subsidize it, at least in the short-run. Therefore, the way government finances its investment in innovation matters.



Finally, all our three policies are capable of generating the medium term business cycles. Even though their effects depend on the way government finances them, in any case they are capable of expand the economy in the medium term. However, their effects crucially depend on the calibration of key parameters, especially those related to labor markets.

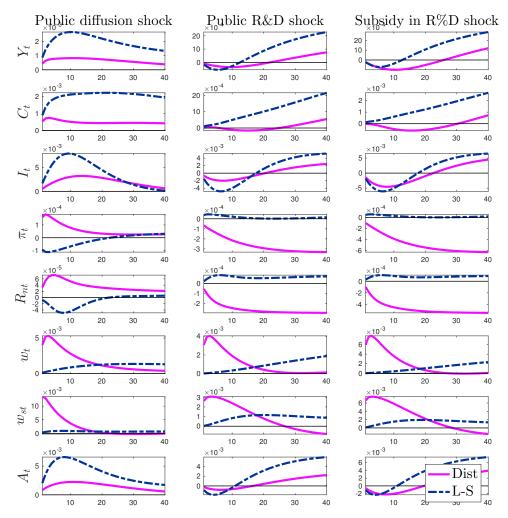


Figure 6: IRF's for shocks to public investment with distortionary taxes and low rigidities  $(\xi_w^* = 0.25\xi_w)$ . Pink solid: distorsionary labor taxes. Blue dashed: lump-sum taxes.

## 5 Conclusion

In this First Work Package we develop a baseline model which serves to analyze the impact of several public innovation policies on the evolution of the economy.

We follow Anzoategui et al. (2015) by including an active role of government policies in the process of R&D and adoption of technologies. We include direct public innovation investment, innovation subsidies, and analyze their effects along with the way they are financed in order to get an intuition of their impact in general equilibrium as well.



We find that public innovation in the form of any of our policies (direct investment or innovation subsidies) expand the economy in the medium term. This implies that it can serve as a substitute for private investment in innovation. We also show that their effects on the economy depend crucially on some parameters, in particular those related with labor markets. We showed that a great degree of wage rigidities hide the aggregate trade-offs generated by labor tax raises. However, even with these trade-offs acting, innovation policies have a positive impact in the aggregate economy, wealth, consumption, and GDP.

This analysis can be extended in several ways. Two important extensions are the following: first, the distributional features of different policies. As they affect different labor markets differently, they have distributional effects; at least in the short term, the skill premium diverges due to these policies. Second, as there are trade-offs of these policies, the evaluation of optimal policy is a natural extension of this framework.

## References

- Aghion, P., Angeletos, G.-M., Banerjee, A., and Manova, K. (2010). Volatility and growth: Credit constraints and the composition of investment. *Journal of Monetary Economics*, 57(3):246 265.
- Anzoategui, D., Comin, D., Gentler, M., and Martinez, J. (2015). Endogenous technology adoption and r&d as sources of business cycle persistence. *Dartmouth mimeo*.
- Barlevy, G. (2007). On the cyclicality of research and development. *American Economic Review*, 97(4):1131–1164.
- Christiano, L. J., Eichenbaum, M., and Evans, C. L. (2005). Nominal rigidities and the dynamic effects of a shock to monetary policy. *Journal of Political Economy*, 113(1):1–45.
- Comin, D. (2009). On the integration of growth and business cycles. *Empirica*, 36:165–176
- Comin, D. and Gertler, M. (2006). Medium-term business cycles. *American Economic Review*, 96(3):523–551.
- Fisher, J. (2015). On the structural interpretation of the smetsouters "risk premium" shock. *Journal of Money, Credit and Banking*, 47(2-3):511–516.
- Griliches, Z. (1990). Patent statistics as economic indicators: A survey. *Journal of Economic Literature*, 28:1661–1707.
- Krishnamurthy, A. and Vissing-Jorgensen, A. (2012). The aggregate demand for treasury debt. *Journal of Political Economy*, 120(2):233–267.
- Romer, P. M. (1990). Endogenous technological change. *Journal of Political Economy*, 98(5, Part 2):S71–S102.





Smets, F. and Wouters, R. (2007). Shocks and frictions in us business cycles: A bayesian dsge approach. *American Economic Review*, 97(3):586–606.

Takahashi, Y., Schmidt, L., Milbradt, K., Dew-Becker, I., and Berger, D. (2016). Layoff risk, the welfare cost of business cycles, and monetary policy. *Northwestern University mimeo*.



## A Log-linearization of returns

The return to R&D,  $R_{t+1}^Z$ . The return to R&D can be obtained from the free-entry condition

$$E_t \left[ \Lambda_{t+1} R_{t+1}^Z \right] = E_t \left[ \Lambda_{t+1} \frac{J_{t+1} \varphi_t}{(1 - \tau_{rt}^s) w_{st}} \right] = 1$$

That loglinearized and detrended is (with  $\hat{x}_t = \log x_t - \log x$ ):

$$\hat{R}_{t+1}^Z = \hat{J}_{t+1} + \hat{\varphi}_t + \tau_{rt}^s - \hat{w}_{st} - \hat{Z}_t + \hat{Z}_{t+1}$$

The return to Diffusion,  $R_{t+1}^A$ . The return to Adoption can be obtained from the value of a new technology:

$$V_t = \pi_t + \phi E_t \{ \Lambda_{t+1} V_{t+1} \}$$

The return becomes:

$$E_t \left[ \Lambda_{t+1} R_{t+1}^A \right] = E_t \left[ \Lambda_{t+1} \phi \frac{V_{t+1}}{V_t - \pi_t} \right] = 1$$

So

$$R_{t+1}^{A} = \frac{\phi V_{t+1}}{V_{t} - \pi_{t}}$$

Which loglinearized and detrended is

$$\hat{R}_{t+1}^A = \hat{V}_{t+1} - \frac{1}{1 - \frac{\pi}{v}} \hat{V}_t + \frac{\frac{\pi}{v}}{1 - \frac{\pi}{v}} \hat{\pi}_t - \hat{A}_t + \hat{A}_{t+1}$$